Radiation absorption and Aligned Magnetic Field effects on MHD Dissipative fluid past an inclined vertical porous plate in Porous media

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Abstract:

In this article, in the presence of the aligned magnetic field, chemical reaction, and radiation absorption results, the research centered on the analysis-free convective flow of a viscous, incompressible, and electrically conducting fluid via an inclined plate through a porous medium. The free stream velocity could obey exponentially increasing small disruption law. Analytically, two-term harmonic and non-harmonic functions overcome non-dimensional governing equations. Distributions of velocity, temperature, and concentration are explored in depth by graphs for different parameter values entering the problem. The skin friction coefficient, heat transfer rate, and mass transfer rate are derived. This research is useful in the steel industry monitoring molten iron flow, nuclear plant liquid metal cooling, and meteorology.

Keywords: Aligned magnetic field, Radiation absorption, MHD, Porous medium, Inclined angle, mixed convective flow.

I. INTRODUCTION

The phenomenon of free convection and mass movement flow of an electrically conducting fluid past an inclined heated surface under the effect of a magnetic field has drawn attention in its application to geophysics, astrophysics and many engineering problems such as cooling of nuclear reactors, aerodynamic boundary layer regulation and cooling towers. Mass transfer is one of the commonly observed phenomena of both chemical and biological sciences. As the fluid is at rest, the mass transfer occurs; mass is transmitted solely through molecular diffusion arising from gradients of concentration. Convective heat and mass transfer mechanism are identical in design with the limited concentration of group in fluid and higher mass transfer speeds. Several studies have also been carried out of simultaneous heat and mass transfer, assuming different physical conditions. In specific chemical engineering methods, the chemical reaction between a foreign mass and the fluid in which the plate lies happens. These processes exist in various industrial applications, including polymer manufacturing, ceramics or glassware processing, and food procession. Mohammed Ibrahim[1] analysed a two-dimensional unstable

Raghunath et al.[10] introduced Hall Effects on MHD Convective Rotating Flow across Endless Vertical Plate Past Porous Medium. Raghunath et al.[12] presented Heat and Mass

Movement of a Visco-Elastic Fluid Past Endless Vertical Oscillating Porous Plate Suresh Babu G et al.[13] mentioned Free Convection Heat Transfer Flow Study in a Vertical Conical Annular Porous Media. Nagendra Prasad et al.[14] studied Visco-elastic fluid MHD flow over an unbounded, rotating porous plate with the heat source and chemical reaction.

Our research focuses on the impact of introducing a second fluid on mixed convection flow. Orphan Aydm et al.[15] had an MHD mixed heat transfer flow across an inclined plate. Reddy et al. researched thermal diffusion and homogeneous chemical reaction results on MHD mixed convection flow with Ohmic heating[16]. Reddy et al. explored unstable MHD radiative, and chemical-reactive natural convection flows near a moving porous plate through a porous medium[17]. Raju et al.[18] considered MHD convective and dissipative fluid flow over porous medium in a flat channel with an isolated and impermeable bottom wall in Joule heating. Ravikumar et al.[19] addressed the combined results of a non-Newtonian fluid's heat absorption and magnet convective movement, namely, Rivlin-Ericksen movement past a semi-infinite vertical porous layer. Raju et al.[20] performed exact solutions for MHD-free convective boundary layer flow past a porous vertical surface in the presence of chemical reaction, thermal radiation, and suction.

In the context of an aligned magnetic field, chemical reaction and radiation absorption results, this analysis focuses on researching the free convective movement of a viscous, incompressible and electrically conducting fluid past an inclined plate via a porous medium. The freestream velocity could obey exponentially increasing small disruption law. Analytically, two-term harmonic and non-harmonic functions overcome non-dimensional governing equations. Distributions of velocity, temperature, and concentration are explored in depth by graphs for different parameter values entering the problem. Skin friction coefficient, heat transfer rate, and mass transfer rate are derived.

II. PHYSICAL AND STATISTICAL FORMULATION

Consider laminar, incompressible, viscous, electrically conducting and heat-absorbing fluid two-dimensional flow past an inclined plate inserted in a porous medium in the presence of chemical reaction and Dufour results. The flow is believed to be in the x-direction, taken around the semi-infinite inclined plate and standard y-axis. A magnetic field of uniform intensity B0 is added at flow path angle α . Free stream velocity meets exponentially increasing small disruption law.

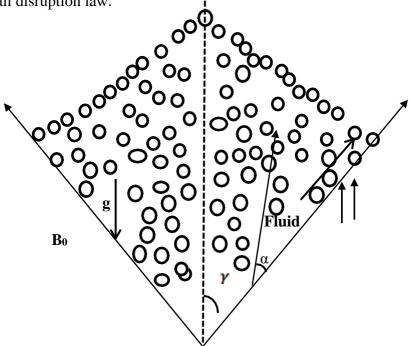


Figure 1: Physical problem-setting

(3)

The governing equations for this investigation are focused on mass, linear momentum, energy and concentration species equilibrium.

and concentration species equinorium.
$$\frac{\partial v^*}{\partial y^*} = 0 \to v^* = -v_0(v_0 > 0) \tag{1}$$

$$v * \frac{\partial u *}{\partial y *} = 9 \frac{\partial^{2} u *}{\partial y *^{2}} + g\beta (T * -T_{\infty}) \cos\alpha + gB^{*} (C * -C_{\infty}) \cos\alpha - \frac{\sigma B^{2}}{\rho} Sin^{2} \gamma u * - \frac{9u *}{k^{*}}$$
(2)

$$v * \frac{\partial T}{\partial y^*} = \frac{k}{\rho C} \frac{\partial^2 T}{\partial y^{*2}} + \frac{9}{C} \left(\frac{\partial u}{\partial y^*} \right)^2 + \frac{\sigma B_0^2}{\rho} u^{*2} + \frac{Q_0}{\rho C} (T^* - T_\infty) + \frac{R^*}{\rho C} (C^* - C_\infty^*)$$

$$v * \frac{\partial C}{\partial y^*} = D \frac{\partial^2 C}{\partial y^{*2}} + -K_1 (C^* - C_\infty)$$

$$v * \frac{\partial C^*}{\partial y^*} = D \frac{\partial^2 C^*}{\partial y^{*2}} + -K_1(C^* - C_{\infty})$$
(4)

The apporpriate boundary conditions for the corresponding fields are

$$u^* = 0$$
 $T^* = T_w$, $C^* = C_w$ at $y^* = 0$

$$u^* \to 0$$
, $T^* \to T_\infty$ $C^* \to C_\infty$ as $y^* \to \infty$ (5)

Introduction of non-dimensional numbers,
$$u = \frac{u^*}{v_0}$$
, $y = \frac{v_0 y^*}{9}$, $\Pr = \frac{9\rho C_p}{k}$, $\theta = \frac{T^* - T_\infty}{T_w - T_\infty}$, $\varphi = \frac{C^* - C_\infty}{C_w - C_\infty}$, $Gr = \frac{9g\beta}{V_0^3}$, $Gr = \frac{9g\beta}$

Where Gr is the Grashof number, Gm is the Grashof number, Pr is the Prandtl number, Sc is the Schmidt number, Ec is the Eckert number, M is the magnetic parameter, Ko is the porous medium and Kr is the chemical reaction parameter.

The simple field EQs (2)-(4) may be represented as non-dimensional.

$$\frac{\partial u^{2}}{\partial y^{2}} + \frac{\partial u}{\partial y} - (M^{2} \sin \gamma + K_{0}) u = -G_{r} \cos \alpha \theta - G_{m} \cos \alpha \varphi$$

$$\frac{\partial^{2} \theta}{\partial y^{2}} + \Pr \frac{\partial \theta}{\partial t} + \Pr E_{c} \left(\frac{\partial u}{\partial y}\right)^{2} + \Pr E c M^{2} u^{2} + \Pr Q \theta + R \varphi = 0$$
(8)

$$Sc\frac{\partial^2 \varphi}{\partial y^2} + \frac{\partial \varphi}{\partial t} - Kr\varphi = 0 \tag{9}$$

The corresponding boundary conditions in dimensionless form are reduced to

At
$$y^* = 0$$
, $u = 0$, $\theta = 1$, $\phi = 1$

As
$$y^* \to \infty$$
, $u \to 0$, $\theta \to 1$, $\phi \to 1$

(10)

Equations (7) - (9) describe a series of partial differential equations that can not be closed. However, it can be reduced to a series of regular, dimensionless differential equations that can be solved analytically. This can be achieved by reflecting tempo, temperature, and concentration.

$$u(y,t) = u_0(y) + E_c u_1(y) + O(Ec^2)$$

$$\theta(y,t) = \theta_0(y) + E_c \theta_1(y) + O(Ec^2)$$

$$\phi(y,t) = \phi_0(y) + E_c \phi_1(y) + O(Ec^2)$$
(11)

Using Equation (11) in Equations (7)–(9) and equating Ec's similar power coefficient

Zero order terms:

$$u'_0 + u'_0 - (M^2 \sin^2 \gamma + K_0) u_0 = -Gr \cos \alpha \theta_0 - Gm \cos \alpha \phi_0$$
 (12)

$$\theta_0' + \Pr(\theta_0)' + \Pr(\theta_0) + \Pr(\theta_0) = 0 \tag{13}$$

$$Sc\phi_0' + \phi_0' - Kr\phi_0 = 0 \tag{14}$$

First order terms:

$$u' + u' - (M^2 \sin^2 \gamma + K) u = -Gr \cos \alpha \theta - Gm \cos \alpha \phi$$

 $\theta' + Pr\theta' + Pr Q\theta = -Pr (u')^2 - Pr M^2 u^2 - R\phi$
(16)

$$Sc\phi_1' + \phi_1' - Kr\phi_1 = 0 \tag{17}$$

Appropriate boundary conditions

$$u_0 = 0, u_1 = 0, \theta_0 = 1, \theta_1 = 0, \phi_0 = 1, \quad \phi_1 = 0$$
 at $y = 0$
 $u_0 \to 0, u_1 \to 0, \theta_0 \to 0, \theta_1 \to 0, \phi_0 \to 0, \phi_1 \to 0$ as $y \to \infty$ (18)

Solving equations (14) - (19) under the boundary conditions (20), the following solutions are obtained

$$\theta_0 = b_1 \exp(-m_1 y) + b_2 \exp(-m_2 y) \tag{19}$$

$$\phi_0 = \exp(-m_1 y) \tag{20}$$

$$u_0 = b_3 \exp(-m_1 y) + b_4 \exp(-m_2 y) + b_5 \exp(-m_3 y)$$
(21)

$$\theta_1 = b_6 \exp(-2m_1 y) + b_7 \exp(-2m_2 y) + b_8 \exp(-2m_3 y) + b_9 \exp(-(m_1 + m_2) y) + b_9 \exp(-(m_1 + m_2)$$

$$\phi_1 = 0 \tag{23}$$

$$u_{1} = b_{13} \exp(-2m_{1}y) + b_{14} \exp(-2m_{2}y) + b_{15} \exp(-2m_{3}y) + b_{16} \exp(-(m_{1} + m_{2})y) + b_{17} \exp(-(m_{3} + m_{2})y) + b_{18} \exp(-(m_{1} + m_{3})y) + b_{19} \exp(-m_{5}y) + b_{20} \exp(-m_{6}y)$$
(24)

The following solutions are obtained under boundary conditions (14) – (19) the velocity, temperature and concentration distribution in the boundary layer as follows

$$u(y,t) = b_3 \exp(-m_1 y) + b_4 \exp(-m_2 y) + b_5 \exp(-m_3 y) + E_c [b_{13} \exp(-2m_1 y) + b_{14} \exp(-2m_2 y) + b_{15} \exp(-2m_3 y) + b_{16} \exp(-(m_1 + m_2) y) + b_{17} \exp(-(m_3 + m_2) y) + b_{18} \exp(-(m_1 + m_3) y) + b_{19} \exp(-m_5 y) + b_{20} \exp(-m_6 y)$$
(25)

$$\theta(y,t) = b_1 \exp(-m_1 y) + b_2 \exp(-m_2 y) + E_c [b_6 \exp(-2m_1 y) + b_7 \exp(-2m_2 y) + b_8 \exp(-2m_3 y) + b_9 \exp(-(m_1 + m_2)y) + b_{10} \exp(-(m_3 + m_2)y) + b_{11} \exp(-(m_1 + m_3)y) + b_{12} \exp(-m_5 y)]$$
(26)

$$\phi(y,t) = \exp(-m_1 y) \tag{27}$$

Skin Friction:

The surface's non-dimensional skin friction $\tau = \left(\frac{\partial u}{\partial y}\right)_{y=0} = \left(\frac{\partial u_0}{\partial y}\right)_{y=0} + E_c \left(\frac{\partial u_1}{\partial y}\right)_{y=0}$ $\tau = -(b_3m_1 + b_4m_2 + bml_3) - E_c[2b_{13}m_1 + 2b_{14}m_2 + 2b_{15}m_3 + b_{16}(m_1 + m_2) + b_{17}(m_3 + m_2) + b_{18}(m_1 + m_2) + b_{18}(m$ $b_{18}(m_1+m_3)+b_{19}m_5+b_{20}m_6)]$

Nusselt Number:

The heat transfer rate in Nusselt is calculated by
$$N_{u} = \left(\frac{\partial \theta}{\partial y}\right)_{y=0} = \left(\frac{\partial \theta_{0}}{\partial y}\right)_{y=0} + E_{c} \left(\frac{\partial \theta_{1}}{\partial y}\right)_{y=0}$$

$$= -(b_{1}m_{1} + b_{2}m_{2}) - E_{c}[2b_{6}m_{1} + 2b_{7}m_{2} + 2b_{8}m_{3} + b_{9}(m_{1} + m_{2}) + b_{10}(m_{3} + m_{2}) + b_{11}(m_{1} + m_{2}) + b_{21}(m_{1} + m_{2}) + b_{22}(m_{1} + m_{2}) + b_{23}(m_{1} + m_{2}) + b_{33}(m_{1} + m_{2})$$

Sherwood Number:

The amount of mass transfer on the wall in Sherwood numbers
$$Sh = \left(\frac{\partial \phi}{\partial y}\right)_{y=0} = \left(\frac{\partial \phi_0}{\partial y}\right)_{y=0} + \left(\frac{\partial \phi_1}{\partial y}\right)_{y=0}$$

$$= -(m_1) (30)$$

4. RESULTS AND DISCUSSION

For computations, the following default parameter values are used in this study: Gr=5.0, α =30, Gm 5.0, Ko=1.0, M=1.0, Pr=0.71, Ec=0.001, Q=0.1, Sc=0.6, Kr=0.1, R=0.5. Therefore, all graphs conform to these values, unless explicitly stated in $\frac{\pi}{6}$, $\frac{\pi}{4}$, $\frac{\pi}{3}$

Velocity Profiles:

Figure 2 indicates the α -inclined angle impact on the velocity profile. We observed the velocity reducing to the inclined angle α values. Figure 3 demonstrates the effects on velocity profile of aligned magnetic field parameter π . We found that the velocity declines as the aligned magnetic field parameter π rises. Figure 4 shows the influence of thermal Grashof number Gr on velocity.

This figure indicates that fluid velocity increases as Gr rises. This is attributed to a buoyancy impact that improves momentum. Figure 5 shows magnetic field influence in velocity spread. The existence of transverse magnetic field renders the fluid flow resistive. This force is called the Lorentz force, which slows down the fluid flow. Figure 6 displays the velocity profiles against the span-wise coordinate in the presence of the permeability parameter. We note that velocity decreases as parameter Ko. Figure 7 displays velocity profiles against changed Grashof number.

We note speed changes as changed Grashof number Gm changes. Figure 8 elucidates the influence of velocity profiles on various chemical reaction parameter (Kr) values. Figure 9 indicates that pace rises as Schmidt number Sc rises. Figure 10 demonstrates the influence of Radiation absorption parameter R on velocity distribution; from this figure, we found that the velocity increases with rises of Radiation absorption parameter. In Figure 11, reversal activity is observed to raise Prandtl number Pr.

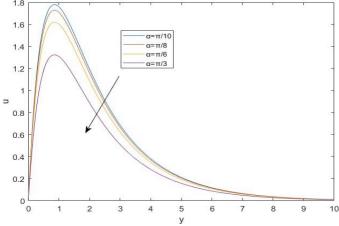


Fig 2: Velocity profiles for different values of α . R=0.5, $\gamma = \pi/6$, Sc=0.6, Pr=0.71, Gr=5,

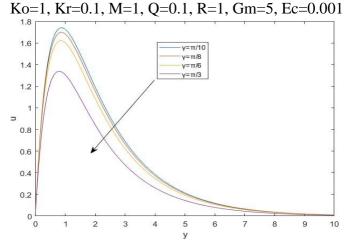


Fig 3: Velocity profiles for different values of α . R=0.5, $\alpha = \pi/6$, Sc=0.6, Pr=0.71, Gr=5,

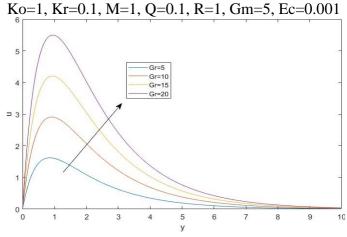


Fig 4: Velocity profiles for different values of Gr. R=0.5, Sc=0.6, Pr=0.71, Ko=1, γ =30, α =30, Kr=0.1, M=1, Q=0.1, R=1, Gm=5, Ec=0.001

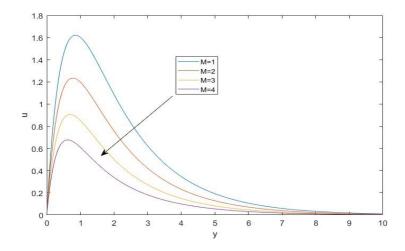


Fig 5: Velocity profiles for different values of M. R=0.5, Sc=0.6, Pr=0.71, Ko=1, γ =30,

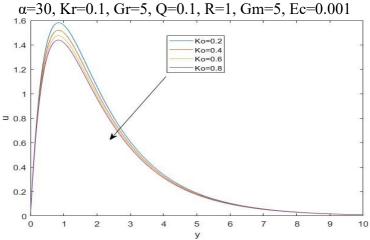


Fig 6: Velocity profiles for different values of Ko. R=0.5, M=1, Sc=0.6, Pr=0.71, α =30, Kr=0.1, γ =30, Gr=5, Q=0.1, R=1, Gm=5, Ec=0.001

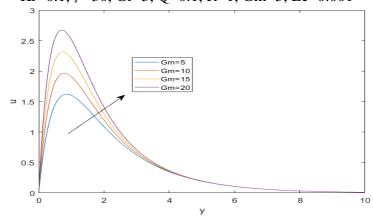


Fig 7: Velocity profiles for different values of Gm. R=0.5, M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, Q=0.1, R=1, Ec=0.001

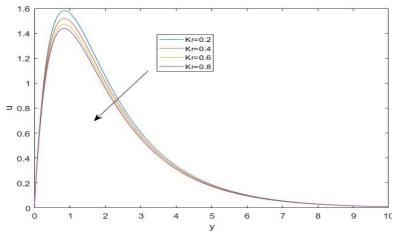


Fig 8: Velocity profiles for different values of Kr. Q=0.5, M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Gr=5, Q=0.1, R=1, Gm=5, Ec=0.001

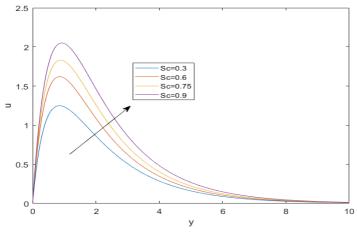


Fig 9: Velocity profiles for different values of Sc. R=0.5, M=1, Pr=0.71, Ko=1, α =30, γ =30,

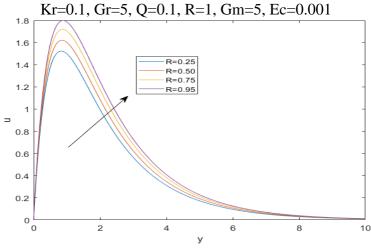


Fig 10: Velocity profiles for different values of R. M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, Q=0.1, R=1, Gm=5, Ec=0.001

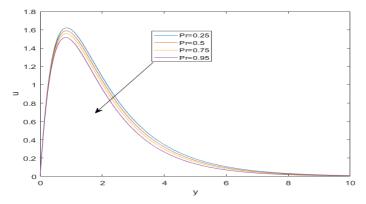


Fig 11: Velocity profiles for different values of Pr. R=0.5, M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, Q=0.1, R=1, Gm=5, Ec=0.001

Temperature Profiles:

Figure 12 demonstrates the influence of heat source parameter Q on temperature distribution—the temperature declines as the heat source parameter Q rises. Figure 13 indicates that temperature declines as Prandtl rises. Figure 14 demonstrates the influence of Radiation absorption on temperature. Temperature is found to raise the Radiation absorption parameter R.

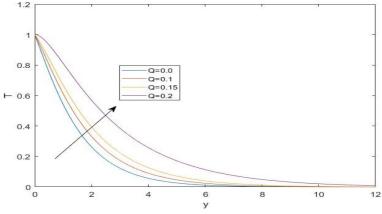


Fig 12: Temperature profiles for different values of Q. R=0.5, M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, R=1, Gm=5, Ec=0.001

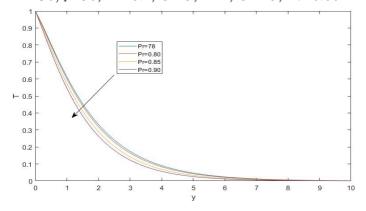


Fig 13: Temperature profiles for different values of Pr. R=0.5, M=1, Sc=0.6, Q=0.1, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, R=1, Gm=5, Ec=0.001

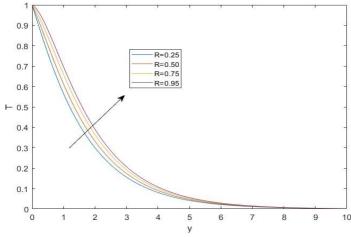


Fig 14: Temperature profiles for different values of R., Q=0.5, M=1, Sc=0.6, Pr=0.71, Ko=1, α =30, γ =30, Kr=0.1, Gr=5, R=1, Gm=5, Ec=0.001

Concentration Profiles:

Figure 15 indicates that the concentration decreases with rising values of the Kr parameter chemical reaction. Figure 16 obvious that the layer thickness of the limit concentration decreases with Sc, and also that the concentration decreases exponentially and enters a free stream state for high Sc values.

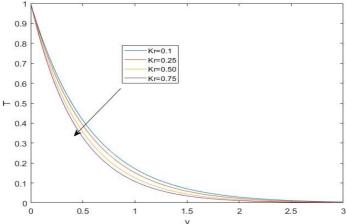


Fig 16: Concentration profiles for different values of Sc

Skin Friction (τ)

Gr	Gm	M	Ko	γ	α	Q	T
5							7.1611
10							10.6733
15							14.1925
	5						7.1611
	10						10.8155
	15						14.4673
		1.5					6.9677
		2					6.4417
		2.5					5.8393
			1				7.1611
			5				3.6578
			7.5				0.3186
				$\pi/10$			0.3187
				π/6			0.3186
				$\pi/3$			0.3185
					$\pi/10$		0.3499
					$\pi/6$		0.3186
					$\pi/3$		0.1840
						0.25	5.0642
						0.50	5.2755
						0.75	5.4549

Nusselt Number (Nu)

Pr	Ec	Q	R	Nu
0.75				-0.6312
0.80				-0.6828
0.85				-0.7342
	1			-0.5879
	5			-0.5810
	10			-0.5724
		0.1		-0.4717
		0.15		-0.5144
		0.20		-0.5366
			0.25	-7.0111
			0.50	-4.6990
			0.75	-2.8333

Sherwood Number (Sh)

Sc	Kr	Sh
0.6		-0.6145
1.2		-1.1013
1.8		-2.5014
	0.001	0.3581
	0.003	0.1430
	0.005	0.0052

Conclusion

The findings of this study are as follows.

- 1. Velocity decreases for increasing values of α , γ , M, Kr, Ko, R and Sc where as it shows reverse tendency in the case of Gr, Gm.
- 2. Temperature distribution decreases with an increase in Pr and (R), where as it is enhances with increasing Q.
- 3. Concentration boundary layer decreases with an increase in Kr and Sc where as it is increases with increasing values of So.
- 4. skin-friction increases with an increase in (Gr), (Gc), (Ko) and (γ) , where as it decreases under the influence of (M) and (α) .
- 5. Nusselt number increases with an Ec, where as it decreases under the influence of (Pr) and (O).
- 6. Sherwood number increases with an increase in So but a reverse effect is noticed in the case of Sc and Kr.

7.

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