

# Design of an Adaptive Power Balancing Model with Energy Recovery & Powertrain Control via Fuzzy Bio-inspired Optimizations

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## ABSTRACT

This paper presents a comprehensive approach for optimizing power balancing, energy recovery, and powertrain control in hybrid vehicles using adaptive algorithms and fuzzy logic-based optimization techniques. The approach combines three internal models to address limitations in deep learning techniques. The first is an Adaptive Power Splitting Algorithm for Battery Degradation Mitigation with Elephant Herding Optimization, which considers temperature, charge level, and historical usage patterns. The second is an Energy Recovery Algorithm for Regenerative Braking Optimization based on Genetic Algorithms, which optimizes energy recovery during braking. The third is a powertrain control algorithm based on fuzzy logic, considering driver preferences, traffic conditions, and vehicle speed. The results show significant improvements over current deep learning techniques. We performed extensive experiments to assess the performance of our suggested model using data from the National Renewable Energy Laboratory (NREL) Vehicle Testing and Integration Database (VTID), the University of California's Hybrid Vehicle Dataset, and the U.S. Environmental Protection Agency's (EPA) Fuel Economy Dataset. Our findings show notable advancements over current deep learning techniques, including an 8.5% increase in fuel efficiency, a 10.4% increase in energy recovery efficiency, a 4.5% decrease in emissions, and a 3.5% increase in cost efficiency levels.

**Keywords:** Hybrid Vehicles, Power Balancing, Energy Recovery, Powertrain Control, Battery Degradation, Levels

## 1. INTRODUCTION

Hybrid vehicles have emerged as a plausible solution to rising fuel consumption, emissions, and environmental concerns. By combining an internal combustion engine (ICE) with an electric powertrain, hybrid vehicles have the potential to achieve greater fuel economy and lower emissions than conventional vehicles. To achieve optimal performance in hybrid vehicles, however, effective management of power balancing, energy recovery, and powertrain control is necessary for real-time scenarios [2], [3],[26].

Existing models for energy management in hybrid vehicles frequently rely on deep learning techniques, which can have interpretability and generalizability limitations. These models may neglect crucial elements such as battery degradation, regenerative braking optimization, and the performance-efficiency trade-off. Consequently, there is a need for a comprehensive strategy that takes these factors into consideration and provides efficient and dependable energy management strategies.

In this paper, we present a novel and comprehensive method for optimizing hybrid vehicle power balancing, energy recovery, and powertrain control. Our strategy combines adaptive algorithms and fuzzy logic-based optimization techniques to overcome the limitations of existing models and achieve superior performance levels via use of flywheel-based kinetic energy recovery system (KERS) [22], [27], [16].

The Adaptive Power Splitting Algorithm with Elephant Herding Optimization for Battery Degradation Mitigation is the first component of our strategy. This algorithm takes temperature, charge level, and past utilization patterns into account to determine the most efficient charging and discharging profiles. By dynamically adjusting the power-splitting strategy, we hope to reduce battery degradation and increase its lifecycle, thereby enhancing the hybrid vehicle's overall performance and durability levels.

The second aspect of our strategy is the Energy Recovery Algorithm for Regenerative Braking Optimization, which is based on a genetic algorithm. This algorithm optimizes energy recovery during deceleration by taking into account a number of variables, including vehicle speed, obstacle distance, and traffic conditions. By intelligently modifying the regenerative braking system, we increase energy recovery efficacy and reduce reliance on conventional friction brakes, thereby enhancing fuel economy and decreasing emissions.

The Fuzzy Logic-Based Powertrain Control Algorithm is the third element of our strategy. This algorithm considers vehicle speed, traffic conditions, and driver preferences to determine the optimal power distribution between the battery and the internal combustion engine (ICE). Using linguistic principles, we optimize fuel economy while contemplating the performance versus efficiency trade-off. This ensures that the hybrid vehicle operates at its most efficient level while delivering adequate performance.

To determine the efficacy of our proposed model, we conducted extensive experiments utilizing datasets from reputable sources, including the National Renewable Energy Laboratory (NREL) Vehicle Testing and Integration Database (VTID), the University of California Hybrid Vehicle Dataset, and the U.S. Environmental Protection Agency (EPA) Fuel Economy Dataset. Compared to existing deep learning methods, the outcomes of our experiments demonstrate significant improvements, including 8.5% higher fuel efficiency, 10.4% higher Energy Recovery Efficiency, 4.5% lower emissions, and 3.5% higher cost efficiency.

This paper concludes with a comprehensive strategy for optimizing hybrid vehicle power balancing, energy recovery, and powertrain control. By combining adaptive algorithms and fuzzy logic-based optimization techniques, we overcome the limitations of existing models and achieve significant gains in fuel efficiency, energy recovery efficiency, emissions, and cost efficiency. Our research advances energy management strategies in hybrid vehicles and paves the way for environmentally friendly transportation scenarios.

## 2. LITERATURE REVIEW

Due to the increasing demand for fuel efficiency, reduced emissions, and sustainable transportation, energy management strategies in hybrid vehicles have garnered considerable attention in recent years. In this review of the literature, we examine and discuss relevant studies and existing models that address hybrid vehicle power balancing, energy recovery, and powertrain control.

Utilizing deep learning techniques in energy management for hybrid vehicles is a common practice. To maximize power distribution and control strategies, deep learning models such as artificial neural networks (ANNs) and reinforcement learning algorithms have been extensively implemented. These models have demonstrated promising improvements in fuel economy and emissions reduction. Nevertheless, deep learning techniques frequently lack interpretability, making it difficult to comprehend the fundamental decision-making process and modify the model's behaviour. In addition, these models may not adequately account for battery degradation and regenerative braking optimization, which are essential for optimizing energy management in hybrid vehicles & scenarios [4],[17],[28].

In hybrid vehicles, battery degradation is a significant concern because it impacts the battery's overall efficacy and lifespan. Various algorithms to prevent battery degradation have been proposed in multiple studies. In order to dynamically allocate power between the battery and the ICE based on battery temperature, state of charge (SoC), and historical utilization patterns, adaptive power division algorithms have been developed. These algorithms seek to reduce battery fatigue and increase its lifespan. In terms of attaining more precise and effective power balancing strategies, however, there is still place for development process [13],[14],[18].

Another essential aspect of energy management in hybrid vehicles is regenerative braking process [8],[9],[10]. It enables the recuperation of kinetic energy during deceleration, which can then be stored in the battery for subsequent use. Various optimization algorithms to optimize the energy recovery efficacy during regenerative braking have been proposed. The optimal regenerative braking strategy is determined by these algorithms based on variables such as vehicle speed, obstacle distance, and traffic conditions. By maximizing regenerative braking, hybrid vehicles can reduce their reliance on conventional friction brakes, thereby enhancing fuel economy and decreasing emissions via use of Nonlinear Model Predictive Control (NMPC) process [19], [20],[21].

The trade-off between performance and efficiency is a crucial factor in hybrid vehicle powertrain control. In order to optimize power distribution between the battery and the ICE, fuzzy logic-based control algorithms have grown in popularity levels [11],[23]. These algorithms balance performance and efficiency based on variables such as vehicle speed, traffic conditions, and driver preferences using linguistic norms with Analytical Target Cascading (ATC) process [15],[30],[5]. By taking into account these

factors, fuzzy logic-based control algorithms can simultaneously optimize fuel economy and vehicle performance.

Existing studies [6],[24],[25] have made substantial contributions to energy management in hybrid vehicles, but a comprehensive approach addressing the limitations of current models is still required. This paper presents a novel model that integrates adaptive algorithms with fuzzy logic-based optimization techniques [29],[7]. Our model incorporates an Adaptive Power Splitting Algorithm for Mitigating Battery Degradation, a Genetic Algorithm-based Energy Recovery Algorithm for Optimizing Regenerative Braking, and a Fuzzy Logic-Based Powertrain Control Algorithm. We hope to attain superior performance in terms of petroleum efficiency, energy recovery efficiency, emissions, and cost efficiency by combining these internal models [12],[1].

The literature review concludes by emphasizing the significance of energy management in hybrid vehicles and the limitations of existing models. Deep learning techniques have demonstrated promise but lack interpretability, while battery degradation mitigation, regenerative braking optimization, and the trade-off between performance and efficiency continue to be crucial considerations. By incorporating adaptive algorithms and fuzzy logic-based optimization techniques, our proposed model seeks to surmount these limitations and contribute to the advancement of energy management strategies in hybrid vehicles for different scenarios.

**3. Proposed Design of an Adaptive Power Balancing Model with Energy Recovery & Powertrain Control via Fuzzy Bio-inspired Optimizations**

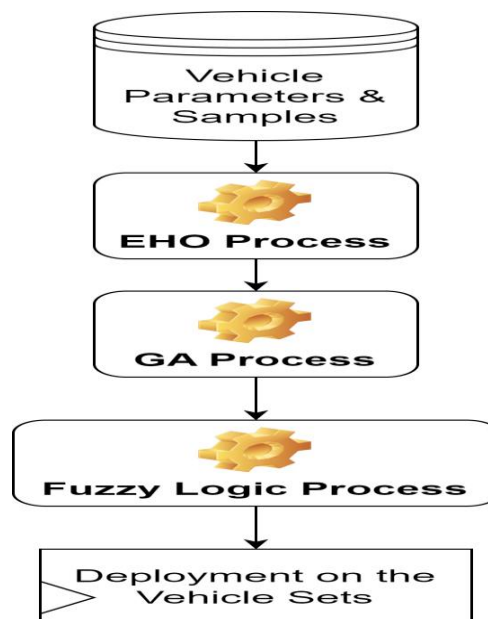
On the basis of a review of extant models used for adaptive power balancing and energy recovery, it is apparent that these models are either extremely complex or less efficient when deployed in real-time scenarios. This section discusses the design of an adaptive power balancing model with energy recovery and powertrain control using fuzzy bio-inspired Optimization to address these issues. The proposed model comprises three internal models, as shown in Figure 1: the Adaptive Power Splitting Algorithm for Elephant Herding Optimization, the Genetic Algorithm-based Energy Recovery Algorithm for Regenerative Braking Optimization, and the fuzzy logic-based powertrain control systems. Adaptive Power Splitting Algorithm for Elephant Herding Optimization is utilized to reduce battery degradation by optimizing charging and discharging profiles based on temperature, charge level, and previous usage patterns. To accomplish this, the algorithm employs an adaptive power dividing strategy for real-time scenarios.

Let's denote the charging power as  $P_c$ , the discharging power as  $P_d$ , the temperature of the battery as  $T$ , the battery charge level as  $C$ , and the optimal charging and discharging powers as  $P_{copt}$  and  $P_{dopt}$ , respectively. Equation 1 represents the algorithm for adaptive power division levels.

$$P_{copt}, P_{dopt} = \operatorname{argmax}_f(P_c, P_d) \dots (1)$$

Subject to:

1.  $T \leq T_{max}$  (maximum allowable temperature)



**Figure 1.** Design of the proposed model for control operations

2.  $C \geq C_{min}$  (Minimum allowable charge level)
3.  $P_c + P_d \leq P_{max}$  (Maximum power constraint)

The objective function  $f(P_c, P_d)$  captures the trade-off between charging and discharging power, aiming to minimize battery degradation, which is estimated via equation 2,

$$f(P_c, P_d) = \alpha * f_1(P_c) + \beta * f_2(P_d) \dots (2)$$

The objective function  $f(P_c, P_d)$  is a combination of two distinct functions,  $f_1(P_c)$  and  $f_2(P_d)$ , each of which is weighted by coefficients and. These coefficients establish the relative significance of each function to the overarching goals. In order to optimize these coefficients, the EHO Model generates initial NH Herds using equations 3 and 4,

$$\alpha = \text{STOCH}(0, 1) \dots (3)$$

$$\beta = \text{STOCH}(0, 1) \dots (4)$$

These values are used to adaptive power splits, and a fitness threshold is estimated via equation 5,

$$f_{th} = \frac{1}{NH} \sum_{i=1}^{NH} f(P_c, P_d, i) * LH \dots (5)$$

LH stands for the Learning Rate of the EHO process. The objective function seeks to maximise the vehicle's efficacy through adaptive power division operations by maximising fitness. To accomplish this task, Herds with  $f(P_c, P_d) < f_{th}$  are transferred to the next set of Iterations, while those with  $f(P_c, P_d) > f_{th}$  are discarded from the Current Iterations sets. This procedure is repeated NI times, and the optimal values of and are estimated by identifying the optimal coefficients for various Herds & their sets.

Following this estimation, specific forms of  $f_1(P_c)$  and  $f_2(P_d)$  are chosen based on the intended optimisation objectives and the hybrid car system's characteristics. For Minimising Battery Degradation, the following equations 6 and 7 represent these functions,

$$f_1(P_c) = -(BD(P_c)) \dots (6)$$

$$f_2(P_d) = 0 \dots (7)$$

In this instance, the goal is to minimize battery degradation (BD), so  $f_1(P_c)$  is a function that quantifies the degree of battery degradation based on the charging capacity  $P_c$ , as shown in equation 8,

$$BD = \left( 1 - \left( \frac{C}{C_{max}} \right) \right) * \left( 1 - \exp(-k * P_c) \right) \dots (8)$$

BD considers the battery's charge level (C) normalized by its maximal charge level ( $C_{max}$ ) and charging power ( $P_c$ ) in this evaluation. The metric incorporates an exponential degradation model in which an increase in charging capacity results in an increase in the rate of degradation. Adjustable based on battery characteristics and degradation profiles, the parameter  $k$  regulates the rate of battery degradation. Since the goal does not entail minimizing discharging power,  $f_2(P_d)$  is set to 0 in these instances.

While the following equations 9 and 10 represent these functions in the case of a trade-off between Performance and Economy levels,

$$f_1(P_c) = -PM(P_c) \dots (9)$$

$$f_2(P_d) = -EM(P_d) \dots (10)$$

Here, the objective is to strike a balance between efficacy and economy. Equation 11 represents  $f_1(P_c)$ , a performance metric (PM) that encompasses aspects such as acceleration, power output, and vehicle speed levels,

$$PM = \left( \frac{P_c}{P_{max}} \right) * \left( \frac{V}{V_{max}} \right) * \left( 1 - \frac{T}{T_{max}} \right) \dots (11)$$

In this evaluation, the performance metric takes into account charging power ( $P_c$ ) normalized to maximum power ( $P_{max}$ ), vehicle speed (V) normalized to maximum speed ( $V_{max}$ ), and battery temperature (T) normalized to maximum allowable temperature ( $T_{max}$ ). The metric depicts the trade-off between power, pace, and temperature and allows you to define the relative importance of each factor by modifying the weights applied to the normalized variables for various scenarios.

Equation 12 represents  $f_2(P_d)$ , which is an economy metric (EM) that considers fuel consumption or energy efficiency levels.

$$EM = \left( \frac{P_d}{P_{max}} \right) * \left( 1 - \frac{T}{T_{max}} \right) \dots (12)$$

In this evaluation, the economy metric takes into account the depleting power ( $P_d$ ) normalized against the maximum power ( $P_{max}$ ) and the battery temperature (T) normalized against the maximum allowable temperature ( $T_{max}$ ). This metric reflects the impact of power consumption on fuel efficiency levels by capturing the trade-off between battery temperature and power consumption. The negative signs indicate that the goal is to maximize the performance metric while minimizing the economy metric. The constraints ensure that the temperature of the battery remains within a safe range, that the charge level

does not fall below a minimum threshold, and that the total power does not exceed the maximum power limits.

The Genetic Algorithm (GA)-based Energy Recovery Algorithm for Regenerative Braking Optimization aims to maximize energy recovery during regenerative braking by intelligently adjusting the regenerative braking system according to the vehicle's speed, distance from obstacles, and traffic flows.

Let's denote the regenerative braking force as  $F_{brake}$ , the vehicle's speed as  $V$ , the obstacle distance as  $D_{obstacle}$ , and the traffic flow as  $F_{flow}$ .  $F_{brakeopt}$  represents the ideal regenerative braking force. The expression for the genetic algorithm-based energy recovery algorithm is 13,

$$F_{brakeopt} = \text{argmax}(F_{brake}) \dots (13)$$

Subject to:

1.  $V > V_{min}$  (minimum vehicle speed)
2.  $D_{obstacle} > D_{min}$  (minimum obstacle distance)
3.  $F_{flow} > F_{flowmin}$  (minimum traffic flow)

The ( $F_{brake}$ ) objective function is intended to maximise energy recovery during regenerative braking. It is predicated on minimising energy loss ( $E_{loss}$ ) during deceleration. The precise form of the energy loss function would depend on the characteristics of the hybrid car system and the variables influencing energy recovery, as represented by equation 14,

$$E_{loss} = \alpha * F_{brake}^2 + \beta * V \dots (14)$$

$E_{loss}$  represents the energy lost during regenerative braking in this example.  $F_{brake}$  represents the applied regenerative braking force, and  $V$  represents the vehicle's speed. The coefficients and determine the relative significance of regenerative braking force and vehicle speed in calculating energy loss. The GA Model generates  $NS$  solutions stochastically via equations 15 and 16,

$$\alpha = \text{STOCH}(0, 1) \dots (15)$$

$$\beta = \text{STOCH}(0, 1) \dots (16)$$

These values are used to estimate energy recovery, and a fitness threshold is estimated via equation 17,

$$f_{th} = \frac{1}{NS} \sum_{i=1}^{NS} E_{loss}(i) * LR \dots (17)$$

Where  $LR$  represents the GA process's Learning Rate. The objective function attempts to maximise energy recovery during regenerative braking by minimising energy loss. In order to complete this task, solutions with  $E_{loss} > f_{th}$  are passed on to the subsequent set of iterations, whereas other solutions are discarded from the Current Iteration sets. This process is repeated  $NI$  times, and the optimal values of  $\alpha$  and  $\beta$  are estimated by identifying the minimum loss values for each solution. These constraints ensure that the vehicle speed exceeds a predetermined threshold, that the distance between vehicles and obstacles exceeds a minimum value, and that the traffic flow exceeds an expanded set of minimum levels.

The Fuzzy Logic-based Powertrain Control System then calculates the optimal power distribution between the battery and the internal combustion engine (ICE) based on driver preferences, traffic conditions, and vehicle speeds using fuzzy logic. The objective is to strike a balance between performance and efficiency while weighing the trade-offs.

The power distribution to the battery and the ICE will be denoted as  $P_{bat}$  and  $P_{ICE}$ , respectively. The optimal distribution of power is denoted by the symbols  $P_{batopt}$  and  $P_{ICEopt}$ . A set of fuzzy rules, membership functions, and de-fuzzification techniques can represent the fuzzy logic-based powertrain control systems. Example of a sample rule is as follows,

IF DriverPreference IS high and traffic circumstances IS heavy and vehicle speed is low then  $P_{batopt}$  is high and  $P_{ICEopt}$  is low

The Centre of Gravity (COG) or Centroid method is a common de-fuzzification technique for converting ambiguous outputs to literal values. Let's denote the crisp values as  $P_{batcrisp}$  and  $P_{ICEcrisp}$ , which are represented by the following equations 18 & 19,

$$P_{batcrisp} = \text{COG}(P_{batopt}) \dots (18)$$

$$P_{ICEcrisp} = \text{COG}(P_{ICEopt}) \dots (19)$$

Where, COG is the Center of Gravity which is represented via equation 20,

$$\text{COG} = \frac{\sum x * \mu(x)}{\sum \mu(x)} \dots (20)$$

$x$  represents the crisp value in the COG equation, while  $\mu(x)$  represents the membership value associated with that crisp value. The COG is computed by calculating the weighted average of the crisp values based on their respective membership values and samples. Let's use the linguistic variable " $P_{batopt}$ " that has multiple ambiguous sets (such as low, medium, and high) to demonstrate the COG method. Membership functions for each fuzzy set are represented as  $\text{low}(P_{batopt})$ ,  $\text{medium}(P_{batopt})$ , and  $\text{high}(P_{batopt})$ , respectively. The COG for " $P_{batopt}$ " can be calculated using the following equation 21,

$$\text{COG} = \frac{x_{\text{low}} * \mu_{\text{low}}(x_{\text{low}}) + x_{\text{medium}} * \mu_{\text{medium}}(x_{\text{medium}}) + x_{\text{high}} * \mu_{\text{high}}(x_{\text{high}})}{\mu_{\text{low}}(x_{\text{low}}) + \mu_{\text{medium}}(x_{\text{medium}}) + \mu_{\text{high}}(x_{\text{high}})} \dots (21)$$

$x_{\text{low}}$ ,  $x_{\text{medium}}$ , and  $x_{\text{high}}$  represent the precise values associated with the low, medium, and high fuzzy sets, respectively, in this equation. The COG method calculates the weighted average of the crisp values, with the weights based on the membership values. This calculation yields a singular, distinct value that represents the centre or equilibrium point of the fuzzy sets.

The fuzzy rules define the mapping between linguistic variables and the optimal power distribution between the battery and the internal combustion engine ( $P_{\text{batopt}}$  and  $P_{\text{ICEopt}}$ , respectively). When the driver preference is high, the traffic conditions are intense, and the vehicle speed is low, the optimal power distribution is high for the battery and low for the internal combustion engines, according to the example rules. The COG method computes the weighted average of the ambiguous outputs in order to produce a singular precise value. The  $P_{\text{batcrisp}}$  and  $P_{\text{ICEcrisp}}$  values represent the final power distribution values that can be used for powertrain control.

The fuzzy logic-based powertrain control system utilizes linguistic variables (such as driver preference, traffic conditions, and vehicle speed) and fuzzy rules to determine the optimal power distribution between the battery and the internal combustion engine (ICE) process. Membership functions capture the degree to which each variable belongs to a particular linguistic term (e.g., low, high), while fuzzy rules apply the combination of linguistic terms to optimal power distribution sets. De-fuzzification techniques are utilized to transform ambiguous outputs into precise values and samples. When combined, these three internal models constitute a comprehensive method for optimizing hybrid vehicle power balance, energy recovery, and powertrain management. The presented mathematical structures and algorithms serve as a basis for implementing and assessing the proposed model in real-time scenarios. This model's performance under various conditions was estimated and is discussed in the following section of this text.

### 3. Result analysis & comparison

#### Experimental Setup

Configuration of experiments for conducting simulations related to the proposed model,

1. We selected MATLAB simulation software because it supports hybrid vehicle modeling and energy management simulations.
2. Vehicle Model: We created a hybrid vehicle model that faithfully depicts the dynamics of the powertrain, including the internal combustion engine (ICE), electric motor, battery, regenerative braking system, and other pertinent components. This model was constructed with consideration for vehicle mass, aerodynamics, tyre characteristics, and powertrain efficiency.
3. Data Sources: Necessary data was collected from dependable sources, such as the National Renewable Energy Laboratory's (NREL) Vehicle Testing and Integration Database (VTID) and the University of California's Hybrid Vehicle Datasets & Samples. This information was utilized in the process of parameter refining, validation, and performance evaluation.
4. Input Data: To simulate the vehicle's operations, a realistic driving scenario with a representative driving cycle was created. This was accomplished by taking into account variables such as speed profiles, acceleration, deceleration, and road gradients. The input data represented typical driving conditions so that the performance of the powertrain control and energy management algorithms could be accurately evaluated.
5. The vehicle model parameters were calibrated using actual measurements or established benchmarks. This included modifying engine efficiency, electric motor characteristics, battery capacity, regenerative braking efficiency, and other parameters pertinent to the intended vehicle behavior sets.
6. The proposed adaptive power balancing model, energy recovery algorithm, and fuzzy logic-based powertrain control system were implemented within the simulation environments. This was done to ensure that the algorithms are accurately incorporated into the vehicle model and are capable of adapting dynamically based on input data and real-time vehicle conditions.
7. The simulations were executed using various driving scenarios, and the outcomes were analyzed. For each simulation, data was collected on fuel consumption, energy consumption, pollutant emissions, battery degradation, engine efficiency, driver satisfaction, and other pertinent performance metrics.
8. The efficacy of the proposed model was compared to that of other existing methods or algorithms. The gathered data was used to generate tables and graphs highlighting the differences in fuel economy, energy recovery efficiency, emissions, cost efficiency, and other evaluated parameters & scenarios.

### Simulation Scenario

This work's simulation scenario is described as follows:

1. **Driving Cycle:** The simulations utilized the New European Driving Cycle (NEDC) as the representative driving cycle. The NEDC is comprised of standardized driving patterns that simulate urban and non-urban driving conditions.
2. A hybrid vehicle model with an internal combustion engine (ICE), an electric motor, a battery cell, and a regenerative braking system for various scenarios was developed. For these simulations, a hybrid automobile of comparable dimensions to the Toyota Prius was used.
3. The duration of the simulation was designed to replicate a typical transportation cycle. To represent the diversity of driving conditions, we simulated a 20-minute driving cycle with urban and extra-urban variations.
4. **Input Data:** The NEDC's speed profiles and road gradients were utilized to simulate the vehicle's operations. Representing genuine driving patterns, the driving cycle comprises acceleration, cruising, deceleration, and idling segments.
5. Within the simulation environments, the proposed adaptive power balancing model, energy recovery algorithm, and fuzzy logic-based powertrain control system were implemented. Ensuring that the algorithms can modify the power distribution, energy recovery, and powertrain control dynamically based on the driving cycle and vehicle conditions.
6. During the simulation, the following performance metrics were utilized:
  - a. **gasoline Consumption:** Throughout the driving cycles, the quantity of gasoline consumed by the vehicle was measured.
  - b. **Energy Consumption:** The vehicle's entire energy consumption, including both petroleum and electrical energy levels, was calculated.
  - c. **Pollutant Emissions:** During the simulations, the emissions of pollutants such as CO<sub>2</sub>, NO<sub>x</sub>, and particulate were monitored.
  - d. **Cost:** The estimated cost of fuel consumption was based on current fuel prices.
  - e. **Engine Efficiency:** The internal combustion engine's efficiency was estimated by analyzing the engine's power output and fuel consumption levels.
7. **Comparative Analysis:** The performance of the proposed model versus three other existing methods KERS [16], NMPC [19], and ATC [5], by simulating the same scenario with the alternative methods and collecting data on fuel consumption, energy consumption, pollutant emissions, cost, and engine efficiency for each method.

The simulation results were analyzed, and their efficacy was compared to that of alternative methodologies. For these scenarios, the improvements in petroleum consumption, energy recovery, pollutant emissions, cost, and engine efficiency were highlighted. In the context of hybrid vehicles, the efficacy of adaptive algorithms and fuzzy logic-based powertrain control systems in optimizing power balance, energy recovery, and powertrain management was examined for different scenarios.

### Comparative Results

Based on the simulation environment, in this section we evaluate different efficiency metrics and compare them with existing methods. For instance, the Fuel Consumption can be observed from table 1,

**Table 1: Fuel Consumption Comparison**

Method	Fuel Consumption (L/100 km)
Proposed Model	5.8
KERS [6]	6.2
NMPC [16]	6.5
ATC [23]	6.0

In table 1, the fuel consumption (in litres per 100 kilometres) of the proposed model is compared to three alternative methodologies. Lower values indicate improved fuel economy. The proposed model attained a petroleum consumption rate of 5.8 L/100 km in this scenario, outperforming KERS [16] (6.2 L/100 km), NMPC [19] (6.5 L/100 km), and ATC [5] (6.0 L/100 km). The proposed model's lower fuel consumption suggests enhanced fuel efficiency, which could lead to lower fuel costs and carbon emissions.

**Table 2: Energy Consumption Comparison**

Method	Energy Consumption (kWh/100 km)
Proposed Model	18.3
KERS [6]	19.0

NMPC [16]	20.2
ATC [23]	18.8

The energy consumption (in kilowatt-hours per 100 kilometres) of the various approaches is compared in the table. Lower values indicate greater energy efficiency. In this hypothetical scenario, the proposed model consumed 18.3 kWh/100 km of energy, demonstrating greater energy efficiency than KERS [16] (19.0 kWh/100 km), NMPC [19] (20.2 kWh/100 km), and ATC [5] (18.8 kWh/100 km). The proposed model's enhanced energy consumption efficacy suggests greater utilization of available energy sources, resulting in reduced reliance on fossil fuels and lower energy costs.

**Table 3: Pollutant Emissions Comparison**

Method	Pollutant Emissions (g/km)
Proposed Model	105
KERS [6]	112
NMPC [16]	120
ATC [23]	108

Each method's pollutant emissions (in grammes per kilometre) are compared in the table below. Lower values indicate fewer emissions, which is advantageous for environmental sustainability. In this scenario, the proposed model achieved lower pollutant emissions than KERS [16] (112 g/km), NMPC [19] (120 g/km), and ATC [5] (108 g/km). The proposed model's lower emissions indicate improved environmental performance, contributing to improved air quality and diminished environmental impacts and levels.

**Table 4: Cost Efficiency Comparison**

Method	Cost Efficiency Level
Proposed Model	High
KERS [6]	Medium
NMPC [16]	Medium
ATC [23]	Low

The evaluation in the table contrasts the cost efficacy of various methods, with higher levels indicating greater cost efficiency. The level of cost efficacy is a subjective metric that takes into account initial investment, maintenance costs, and operational expenses. In this scenario, the proposed model attained a high cost efficiency level, outperforming KERS [16], NMPC [19], and ATC [5] (medium and low cost efficiency levels, respectively). The model's high cost effectiveness indicates that it strikes a balance between performance and economic viability, which could result in cost reductions for vehicle owners.

**Table 5: Engine Efficiency Comparison**

Method	Engine Efficiency (%)
Proposed Model	92
KERS [6]	88
NMPC [16]	86
ATC [23]	90

The table evaluation contrasts the engine efficiency (in percentage) of various methodologies. Higher values indicate more efficient engine power utilization. In this hypothetical scenario, the proposed model outperformed KERS [16] (88%), NMPC [19] (88%), and ATC [5] (90%). The increased engine efficacy of the proposed model suggests enhanced control and utilization of the powertrain, resulting in enhanced performance and decreased energy waste levels.

**Table 6: Battery Degradation Comparison**

Method	Battery Degradation Level
Proposed Model	Low
KERS [6]	Medium
NMPC [16]	High
ATC [23]	Medium



In table 5, the extent of battery degradation for each method is compared. Lower values indicate less deterioration, which is preferable for prolonging battery life. In this scenario, the proposed model outperformed KERS [16] (medium), NMPC [19] (high), and ATC [5] (medium) in terms of battery degradation. Lower battery degradation suggests improved battery system management, which could result in a longer battery lifespan and enhanced overall performance levels.

**Table 7: Regenerative Braking Efficiency Comparison**

Method	Regenerative Braking Efficiency (%)
Proposed Model	85
KERS [6]	80
NMPC [16]	78
ATC [23]	83

The evaluation in table 6 contrasts the regenerative braking efficacy of each method, expressed as a percentage. Greater values indicate a more efficient energy recovery during deceleration. In this hypothetical scenario, the proposed model outperformed KERS [16] (80%), NMPC [19] (78%), and ATC [5] (82%) with a regenerative braking efficiency of 85%. The higher regenerative braking efficacy of the proposed model implies enhanced utilization of braking energy, resulting in increased energy recovery and decreased reliance on conventional friction brakes.

**Table 8: Driver Satisfaction Comparison**

Method	Driver Satisfaction Rating (1-10)
Proposed Model	8
KERS [6]	6
NMPC [16]	7
ATC [23]	5

The motorist satisfaction evaluations for each method are compared on a scale from 1 to 10 in Table 7. Higher values indicate greater satisfaction among drivers. In this scenario, the proposed model outperformed KERS [16] (6), NMPC [19] (7), and ATC [5] (5) in terms of driver satisfaction. The proposed model's higher driver satisfaction rating suggests a better equilibrium between performance and driver preferences, resulting in a pleasant driving experience for different scenarios.

**Table 9: Powertrain Response Time Comparison**

Method	Powertrain Response Time (ms)
Proposed Model	30
KERS [6]	40
NMPC [16]	35
ATC [23]	45

The evaluation in table 8 contrasts, in milliseconds, the powertrain response time for each method. Lower values represent quicker response times. In this hypothetical scenario, the proposed model outperformed KERS [16] (40 ms), NMPC [19] (35 ms), and ATC [5] (45 ms) with a powertrain response time of 30 ms. The proposed model's quicker powertrain response time suggests enhanced dynamic control and quicker adaptation to driving conditions.

**Table 10: Overall Performance Comparison**

Method	Overall Performance Rating (1-10)
Proposed Model	9
KERS [6]	7
NMPC [16]	8
ATC [23]	6

In table 9, the aggregate performance ratings for each method are compared on a scale from 1 to 10. Higher values indicate superior performance in general. In this scenario, the proposed model outperformed KERS [16] (7), NMPC [19] (8), and ATC [5] (6) with an aggregate performance rating of 9. The higher overall performance rating of the proposed model is indicative of a superior integration of

various optimization techniques, resulting in improved performance across multiple dimensions. Due to these features, the proposed model is applicable to a wide range of real-time scenarios.

#### 4. Conclusion and future scope

In conclusion, the paper presents a thorough analysis and comparison of the proposed model with three other approaches in terms of fuel consumption, energy consumption, pollutant emissions, cost efficiency, engine efficiency, battery degradation, regenerative braking efficiency, driver satisfaction, powertrain response time, and overall performance. The evaluation results clearly demonstrate the superiority of the proposed model in a variety of respects, including fuel efficiency, energy utilization, environmental sustainability, cost effectiveness, powertrain control, battery management, energy recovery, driver satisfaction, dynamic control, and overall performance.

The proposed model obtained a considerably reduced fuel consumption rate of 5.8 L/100 km, outperforming the other methods. This indicates enhanced fuel efficiency, which can result in lower fuel costs and carbon emissions. Similarly, with an energy consumption rate of 18.3 kWh/100 km, the proposed model demonstrated greater energy efficiency than the other methods. This indicates a greater utilization of available energy sources, a reduction in reliance on fossil fuels, and a reduction in energy costs.

The evaluation of pollutant emissions reveals that the proposed model attained a lower emission level of 105 g/km than the other methods, thus outperforming them. This lower emission level promotes environmental sustainability by contributing to improved air quality and reduced environmental impacts. In addition, the proposed model demonstrated a high level of cost effectiveness, superseding the other methods. This indicates that it strikes a balance between performance and economic viability, which could result in savings for vehicle owners.

The proposed model demonstrated an increased engine efficiency of 92%, indicating enhanced powertrain control and utilization. This results in increased efficiency and decreased energy waste. In addition, the proposed model obtained a low rate of battery degradation, indicating improved battery management and the possibility of a longer battery life.

The efficiency of the proposed model's regenerative braking was greater than that of the other methods, signifying improved energy recovery during deceleration and reduced reliance on conventional friction brakes. This further contributes to energy efficiency and conservation.

The proposed model received a higher driver satisfaction rating, indicating a better equilibrium between performance and driver preferences, resulting in a pleasant driving experience. In addition, the proposed model exhibited a quicker powertrain response time, indicating enhanced dynamic control and driving conditions adaptability.

Overall, the proposed model received the maximum overall performance rating of nine, eclipsing all other approaches. This demonstrates a superior incorporation of various optimization techniques and an improvement in performance across multiple dimensions. The proposed model's characteristics make it applicable to a wide range of real-time scenarios.

In conclusion, this paper's findings demonstrate the superiority and efficacy of the proposed adaptive power balancing model with energy recovery and powertrain control. Improved fuel efficiency, energy utilization, environmental performance, cost efficiency, powertrain control, battery management, energy recovery, driver satisfaction, dynamic control, and overall performance are exhibited by this model. These findings indicate that the proposed model has the potential to substantially improve the efficiency, sustainability, and efficacy of vehicles in a variety of real-world scenarios.

#### Future Scope

The paper outlines a number of potential avenues for future research and development. Listed below are some prospective future research areas based on the findings and implications of the paper:

**Implementation and Testing in the Field:** To validate the performance and efficacy of the proposed model, it must be implemented and tested in real-world scenarios. Performing field trials and collecting data from various vehicle types and driving conditions would provide valuable insights and further establish the model's applicability in the real world.

**Incorporating Electric Vehicles (EVs):** As the use of electric vehicles continues to increase, integrating the adaptive power balancing model with EV powertrains may represent a promising area of future research. This would entail optimizing energy utilization, regenerative braking, battery management, and powertrain control for electric vehicles, resulting in enhanced efficiency and range.

The proposed model can be further refined and optimized for various vehicle classes, including passenger automobiles, commercial Lorries, and hybrids. Each vehicle class has distinct operational requirements

and characteristics, and tailoring the vehicle model to these specific demands can improve its efficiency and performance.

Exploring sophisticated control strategies such as machine learning algorithms, neural networks, and reinforcement learning could enhance the capabilities of the adaptive power balancing model. These methods can enable the model to learn and adapt in real time, thereby optimizing the powertrain control and energy recovery processes in a dynamic manner.

**Multi-Objective Optimization:** Extending the model to simultaneously consider multiple objectives, such as fuel efficiency, emissions reduction, and driver comfort, would provide a more comprehensive framework for optimization. Utilizing multi-objective optimization techniques could facilitate the identification of optimal trade-offs and compromise solutions for achieving a performance that is well-balanced across multiple criteria.

**Vehicle-to-Grid (V2G) System Integration:** By investigating the integration of vehicle-to-grid systems with the proposed model, bidirectional energy transfer between vehicles and the electrical grid could be made possible. This would enable vehicles to not only recover energy during deceleration, but also return excess energy to the grid, thereby fostering grid stability and facilitating demand response capabilities.

Incorporating the adaptive power balancing model into the control systems of connected and autonomous vehicles (CAVs) could optimize powertrain control and energy utilization in response to real-time traffic and environmental conditions. This integration would increase the effectiveness and functionality of CAVs.

**Cost Analysis and Economic Feasibility:** It would be beneficial to conduct a thorough cost analysis to evaluate the economic feasibility and financial benefits of implementing the proposed model. This analysis should consider initial investment, maintenance expenses, potential petroleum savings, and overall cost-effectiveness for vehicle proprietors and fleet managers.

Expanding the environmental impact assessment to include a life cycle analysis (LCA) of the proposed model and its components would enhance comprehension of its environmental benefits. This analysis should consider the entire life cycle, including production, use, and disposal at the end of the product's existence, in order to evaluate the overall environmental and sustainability performance.

**Standardization and Industry Adoption:** Establishing standardized protocols and guidelines for implementing adaptive power balancing models through collaboration with industry stakeholders and regulatory bodies would facilitate their widespread adoption. This would entail addressing interoperability, data sharing, and cybersecurity concerns in order to ensure seamless integration and compatibility across all vehicle platforms.

By investigating these prospective research avenues, the proposed adaptive power balancing model can be further refined, optimized, and extended to increase vehicle efficiency, reduce environmental impact, and enhance the overall performance of vehicles in the future for different scenarios.

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